## Cryptographic protocols. Functionality for secure channels.

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## 1 Introduction

We have an predefined functionality F, which provides secure channels for n parties. Our new functionality must not allow reordering of the messages, an adversary A, who can decide when the message will reach it's destination will be obliged to transmit the messages in the correct order, otherwise the protocol will fail. Also we have to forbid duplication of the messages. In other words  $M_i$  and  $P_i$  will accept same message only once and reject duplicates.

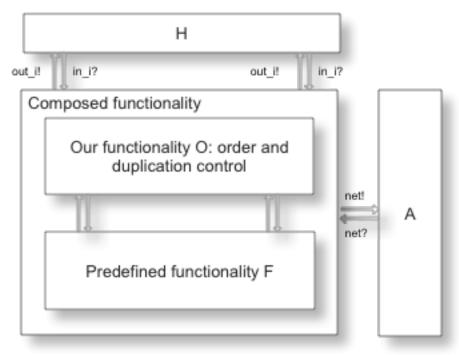


Figure 1. Composed functionality we want to build.

## 2 Ordering and duplication control

Functionality F includes objects  $M_1^F \dots M_n^F$  which provide functions needed for secure message exchange.  $M_i^F$  is controlled by  $P_i$ ,  $P_i$  send a task to the  $M_i^F$  through  $in_i$  and after this task is complete  $M_i^F$  responds through  $out_i$  back to the  $P_i$ . Our goal is to preserve the order of those messages and somehow make them unique, to avoid duplication. Our functionality O also includes object  $M_1^O \dots M_n^O$  which add the following function to the system: each  $M_i$  has two sets of counters  $counter_1^{in_i} \dots counter_n^{in_i}$  and  $counter_1^{out_i} \dots counter_n^{out_i}$ , they count how many messages were received from  $M_j$  and how many were sent to  $M_j$ . When  $P_i$  want to send message m to  $P_j$  then  $P_i$  gives the task to  $M_i^O$ ,  $M_i^O$  appends  $counter_j^{out_i}$  to the message, increments

 $counter_j^{out_i}$  and forwards it to the  $M_i^F$  it, which securely sends it to the  $M_j^F$ , it forwards the message to the  $M_j^O$  and here  $M_j^O$  checks if appended  $counter_j^{out_i}$  equals  $counter_i^{in_j}$ . If equals, then everything is OK and we can forward message to the  $M_j$  and increment  $counter_i^{in_j}$ . The whole scheme looks as follows:

- 1.  $P_i$  send (m,j) to  $M_i^O$
- 2.  $M_i^O$  send  $(m||counter_j^{out_i}, j)$  to  $M_i^F$ , increment  $counter_j^{out_i}$
- 3.  $M_i^F$  send  $(m||counter_j^{out_i}, j)$  to  $M_j^F$
- 4.  $M_j^F$  send  $(m||counter_j^{out_i}, j)$  to  $M_j^O$
- 5.  $M_j^O$  check if  $counter_j^{out_i} = counter_i^{in_j}$ 
  - equal:  $M_j^O$  send (m) to  $P_j$ , increment counter  $i^{inj}$
  - not equal: do nothing

Such approach does not allow to break the order of the messages, because the receiver will wait until he gets correct message and drop all other messages. And if we try to send one message twice, it will be rejected, because counter, which counts incoming messages is already incremented.